

PROBLEM SOLVING IN ACTION

GRADE 2



Presenter
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OVERVIEW

Learning Intention:

- Fostering higher expectations for all learners to accelerate student achievement

I can statements:

- I can participate in problem solving protocols.
- I can share strategies for teaching problem solving.



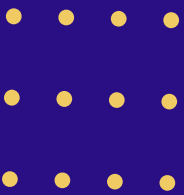


TURN AND TALK



Let's
Talk

What strategies and/or resources are you currently using to teach problem solving in your classroom?



KEY

POINT

The primary goal of problem solving is
making sense of mathematics!



Key Words:


Key words are **NOT** a viable strategy for solving word problems. **Instead, we want students to make sense of problems and make use of their understanding to solve the problems.** Moreover, research tells us that the use of key words as a strategy for solving problems adds to our students' inability to solve problems.





MATHEMATICAL PROCESS STANDARD #1

Make sense of problems and persevere in solving them.

- 
- a. Relate a problem to prior knowledge.
 - b. Recognize there may be multiple entry points to a problem and more than one path to a solution.
 - c. Analyze what is given, what is not given, what is being asked, and what strategies are needed, and make an initial attempt to solve a problem.
 - d. Evaluate the success of an approach to solve a problem and refine it if necessary.

WHAT DOES IT LOOK LIKE WHEN STUDENTS MAKE SENSE OF PROBLEMS?



<https://www.youtube.com/watch?v=kibaFBgaPx4>



MATH SCCCR STANDARDS PROGRESSION (2ND)

2.ATO.1 Solve one- and two-step real-world/story problems using addition (as a joining action and as a part-part-whole action) and subtraction (as a separation action, finding parts of the whole, and as a comparison) through 99 with unknowns in all positions.

2.MDA.7 Solve real-world/story problems involving dollar bills using the \$ symbol or involving quarters, dimes, nickels, and pennies using the ¢ symbol.

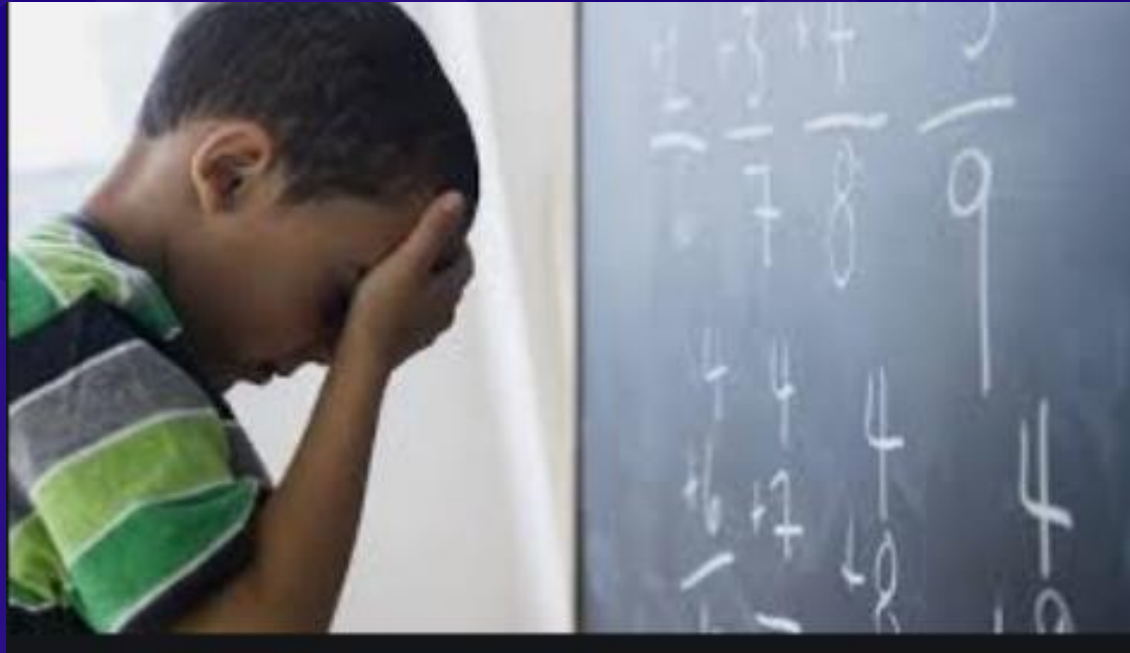
Types of Problems (+, -)

Common Addition and Subtraction Problem Types

	Result Unknown	Change Unknown	Start Unknown
Add to/ Joining	Two bunnies sat on the grass. Three more bunnies hopped there. How many bunnies are on the grass now? $2 + 3 = ?$	Two bunnies were sitting on the grass. Some more bunnies hopped there. Then there were five bunnies. How many bunnies hopped over to the first two? $2 + ? = 5$	Some bunnies were sitting on the grass. Three more bunnies hopped there. Then there were five bunnies. How many bunnies were on the grass before? $? + 3 = 5$
Joining action-involves three quantities; an initial amount, a change amount (the part being added or joined), and the resulting amount (the amount after the action is over).			
Take From/ Separating	Five apples were on the table. I ate two apples. How many apples are on the table now? $5 - 2 = ?$	Five apples were on the table. I ate some apples. Then there were three apples. How many apples did I eat? $5 - ? = 3$	Some apples were on the table. I ate two apples. Then there were three apples. How many apples were on the table before? $? - 2 = 3$
Separation action involves three quantities; the initial amount as the whole or the largest amount, a change, and result amounts.			
	Total Unknown	Addend Unknown	Both Addends Unknown
Part-Part- Whole	Three red apples and two green apples are on the table. How many apples are on the table? $3 + 2 = ?$	Five apples are on the table. Three are red and the rest are green. How many apples are green? $3 + ? = 5, 5 - 3 = ?$	Grandma has five flowers. How many can she put in her red vase and how many in her blue vase? $5 = 0 + 5, 5 = 5 + 0$ $5 = 1 + 4, 5 = 4 + 1$ $5 = 2 + 3, 5 = 3 + 2$
Part-Part-Whole action-involves two parts that are combined into one whole. There is no meaningful distinction between the two parts within a part-part-whole situation, so there is no need to have a different problem for each part as the unknown.			
	Difference Unknown	Bigger Unknown	Smaller Unknown
Compare	<p>["How many more?" version]: Lucy has two apples. Julie has five apples. How many more apples does Julie have than Lucy?</p> <p>["How many fewer?" version]: Lucy has two apples. Julie has five apples. How many fewer apples does Lucy have than Julie? $2 + ? = 5, 5 - 2 = ?$</p>	<p>["Version with "more"]: Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have?</p> <p>["Version with "fewer"]: Lucy has 3 fewer apples than Julie. Lucy has two apples. How many apples does Julie have? $2 + 3 = ?, 3 + 2 = ?$</p>	<p>["Version with "more"]: Julie has three more apples than Lucy. Julie has five apples. How many apples does Lucy have?</p> <p>["Version with "fewer"]: Lucy has 3 fewer apples than Julie. Julie has five apples. How many apples does Lucy have? $5 - 3 = ?, ? + 3 = 5$</p>

Compare problems involve the comparison of two quantities, and the third amount is the difference between the two amounts. (Adapted from Van de Walle)

MANY STUDENTS THINK WORD PROBLEMS ARE HARD!



WHY ARE WORD PROBLEMS SO HARD?

Issue #1: Reading Levels (Student's Level)

"...mathematics text contain more concepts per sentence and paragraph than any other type of text. They are written in a very compact style; **each sentence contains a lot of information**, with little redundancy."

- Barton & Heideman, 2002



WHY ARE WORD PROBLEMS SO HARD?

Issue #2: Answer-Getting Mind Sets

Phil Daro says...

Why give students problems to solve?

1. To learn mathematics!

2. Answers are part of the process, they are not the product.

- The product is the student's mathematical knowledge and know-how.
- The "correctness" of the answers is only part of the process.





WHY ARE WORD PROBLEMS SO HARD?

Issue #3: Over simplification of the problem solving process

Problem Solving Steps to Success


- Read over the problem twice.
- Underline or highlight the question.
- Choose an appropriate strategy to solve the problem.
- SOLVE**
Draw a picture, make a chart, write out your calculations.
- SHOW ALL OF YOUR WORK!**
- Answer the question in a complete sentence.
- Explain your thinking ("I know because...") and tell how you solved the problem.
- Check over your answer and ask yourself "Does my answer make sense?"

STEPS for Solving Word Problems

- 1. Read the problem carefully.**

- 2. Underline the facts you will need to solve the problem.**

- 3. Draw a picture, if needed, to help you solve the problem.**

- 4. Write a number sentence for the problem.**
 $2 + 2 =$
- 5. Solve the problem. Show your work.**
 $2 + 2 = 4$
- 6. Check your answer.**



Problem Solving Read and Think

Understand



Plan

Choose a Strategy



Do

Solve the Problem

 $3 + 3 + 3 = 9$

Check

Explain Your Work

"I made three hops of 3 on the number line"

Problem Solving Model

Read It!
1 UNDERSTAND THE PROBLEM

- Read the problem 2, maybe 3 times. Highlight or underline important information.
- Talk it! - talk about the problem to understand it better.

Think It!
2 MAKE A PLAN

- What strategy will you use and why?
- Talk it! - discuss strategies with a partner.
- What manipulatives will you use?

Solve It!
3 CARRY OUT THE PLAN

- Apply your strategy.
- You may need to revise and try a different strategy....
- Show your work (thinking).
- Ask yourself...
 - Is your answer reasonable?
 - Does it make sense?

Explain It!
3 COMMUNICATE THE SOLUTION

- Answer the question!
- Tell, show, write... how the answer was reached. Consider extensions.
- First I... I noticed that... Then I... I thought... Finally...

KEY MESSAGES



The teacher's role as facilitator is crucial in the delivery of an effective problem-solving experience.

So what can we do?



DISTRICT PROBLEM SOLVING PROTOCOLS

Mathematics Problem-Solving Protocol
K-2

R READ the problem carefully.	I ILLUSTRATE DRAW a picture, diagram, or use a manipulative.	S SOLVE USE your math strategies.	E EXPLAIN JUSTIFY your answer.
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Richland School District One



Mathematics Problem-Solving Protocol
3-5

R READ the problem carefully.	I ILLUSTRATE DRAW a picture, diagram, or use a manipulative.	S SOLVE USE your math strategies.	E EXPLAIN JUSTIFY your answer.
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The Department of
Elementary Education
Richland School District One



So what can we do?

1. Assess where students 'break-down' when problem solving
2. Select a manageable and achievable goal(s) or focus area(s)
3. Implement research-based strategies to address and target areas of challenge
4. Assess and celebrate progress

STRATEGY #1 **3**READ PROTOCOL

- 1st Read: **Read for key ideas.** (understanding)
- Students read or listen to the problem to understand the math.

No pencils...



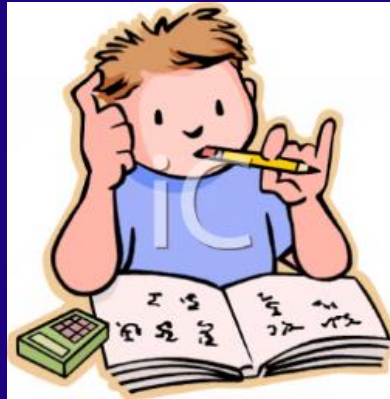
3 READ PROTOCOL

- 2nd Read: Read to understand the math.
- Students read to make sense of what is happening. What are some of the numbers represented in the problem? What do the numbers mean?



3 READ PROTOCOL

- 3rd Read: Read to make a plan.
- Students read to make a plan on solving the problem. What is the question? How can I solve this problem? Are there manipulatives that I can use?



3 READ PROTOCOL IN ACTION

Faye picked 21 tulips and 41 roses to make flower bouquets. If she only used 16 of the flowers, how many flowers are left?



THINK-PAIR-SHARE

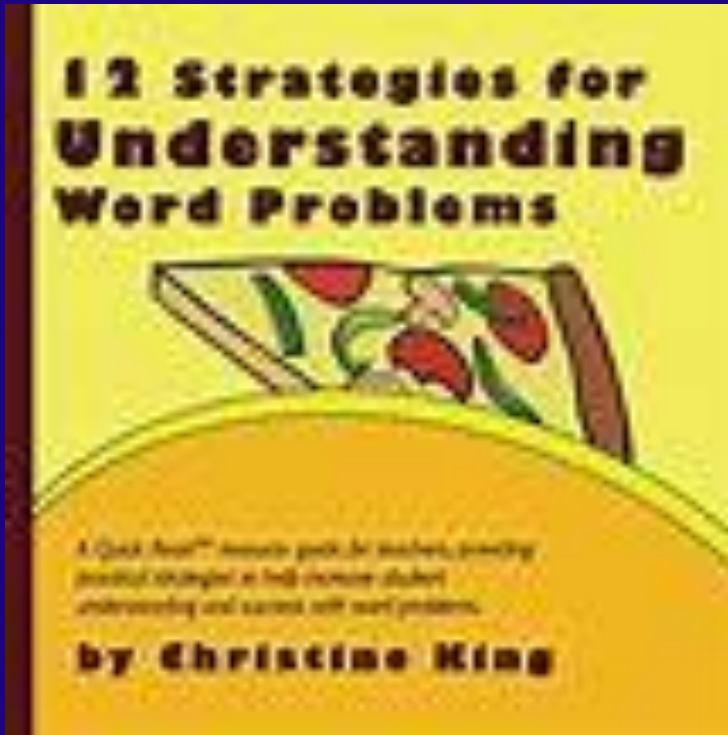


- What are some benefits of a 3 Read Protocol in a math classroom?

Let's
Talk

12 STRATEGIES FOR UNDERSTANDING WORD PROBLEMS

By Christine King



- ❑ Word Problem Puzzle
- ❑ A Line at a Time
- ❑ What is the Question



WORD PROBLEM PUZZLE

12 Strategies for
Understanding
Word Problems



A Good and Beautiful™ resource pack for teachers, covering
practical strategies to help increase student
understanding and success with word problems.

by Christine King

#1 Word Problem Puzzle

Task:

1. A word problem is cut apart as separate sentences into strips of paper.
2. Students have to put the strips in the correct order.
3. Students then solve the problem.

Put this word problem in order.

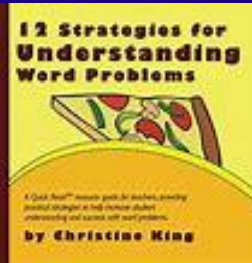
Tina has 6 fewer pieces of candy than Tony.

Tina also has some Skittles.

How many pieces of candy does Tina have?

Tony has 18 Skittles.

WORD PROBLEM PUZZLE IN ACTION



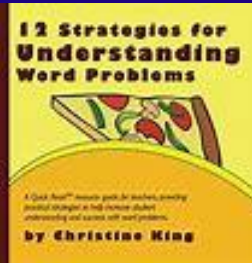
Now there are 60 students in the cafeteria.

How many students were in the cafeteria to start with?

Some students are in the cafeteria.

24 more students came in.

WORD PROBLEM PUZZLE IN ACTION



Some more crawled in.

How many ladybugs crawled into the garden?

There are 62 ladybugs in the garden.

Now there are 82 ladybugs.

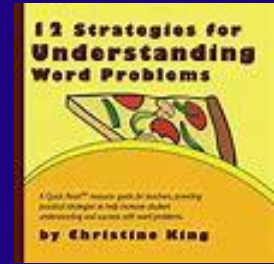
THINK-PAIR-SHARE



- What are some benefits of using Word Problem Puzzle Protocol?



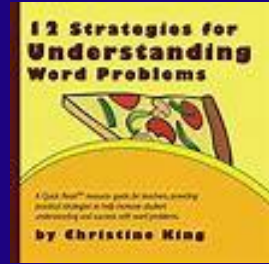
A LINE AT A TIME



Word problems are revealed one sentence at a time. As each line is revealed have students discuss and visualize the information and how that information connects to what they already know.

A LINE AT A TIME

On Monday morning, there were 32 birds in the cage at the pet shop.

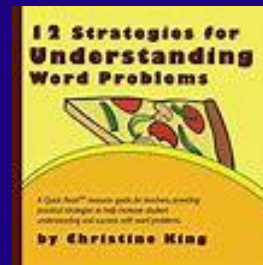


Visualize



A LINE AT A TIME

By Monday afternoon, 22 birds had been sold.

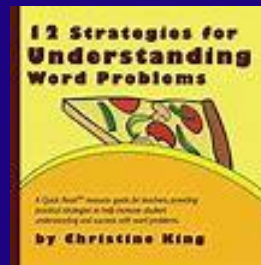


Visualize



A LINE AT A TIME

How many birds were still in cages?



Visualize

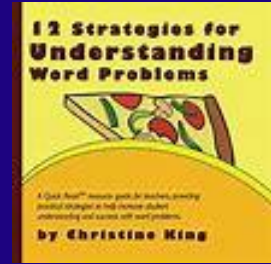


A LINE AT A TIME

On Monday morning, there were 42 birds in the cage at the pet shop.

My Monday afternoon, 22 birds had been sold.

How many birds were still in cages?



Visualize



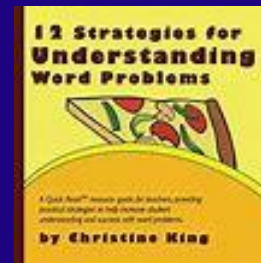
THINK-PAIR-SHARE



- What are some benefits of A Line At A Time Protocol?



WHAT IS THE QUESTION?



- Take a word problem and remove the question. Students have to come up with questions that could be answered based upon the context or situation.





12 Strategies for Understanding Word Problems



A Quick Start™ resource guide for teachers providing practical strategies to help increase student understanding and success with word problems.

by Christine King

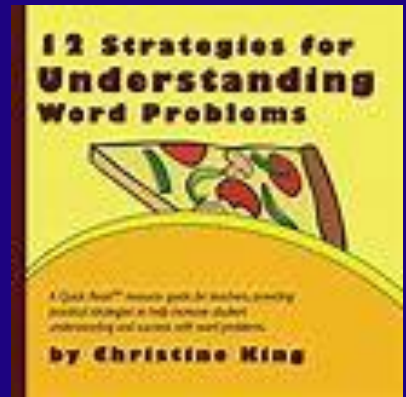
Robin was playing a number's game. In the first round she scored 32 points and in the second round she scored 21 points. In the last round she lost 8 points.



WHAT IS THE QUESTION.

Mrs. Martin wanted her students to practice comparing numbers so they would be prepared for their math test on Friday. She asked Jonathan to draw 3 numbers out of a paper bag. He drew the numbers below.

4 8 5



THINK-PAIR-SHARE



- What are some benefits of using What is the Question Protocol?



GRAPHIC ORGANIZERS & PROBLEM SOLVING



RISE

Mathematics Problem-Solving Protocol

3-5

R

READ

READ
the
problem
carefully.



I

ILLUSTRATE

DRAW
a picture,
diagram, or
use a
manipulative.



S

SOLVE

USE
your
math
strategies.



E

EXPLAIN

JUSTIFY
your
answer.



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READ	ILLUSTRATE
Read the problem carefully	Draw a picture, diagram or use a manipulative.
RISE	
SOLVE	EXPLAIN
Use your math strategies.	Justify your answer.

Two Step Graphic Organizer

Anna bought 3 packs of stickers. Each pack had 5 stickers. Then Anna's friend gave her 10 more stickers. How many stickers does Anna have now?

Name _____

Two Step Template

My First Step

Show It

Equation

My Second Step

Show It

Equation

THINK-PAIR-SHARE



- How can graphic organizers help students' problem solve?
- Are there other graphic organizers that your school is currently using to help with problem solving?



WHEN CHILDREN PRACTICE EFFECTIVE PROBLEM-SOLVING STRATEGIES, THEY REAP MANY BENEFITS:

- apply, understand and practice skills in context;
- collaborate with others to develop new strategies;
- formulate and test their own explanations;
- communicate their explanations and listen to others' explanations;
- use flexible representations to help them solve problems.



HOW DO WE FIND ADDITIONAL PROBLEM-SOLVING TASKS FOR STUDENTS?

All K-5 Math units include at least 1 problem solving task.





Let's
talk.

**TAKE A MOMENT TO THINK ABOUT
YOUR EXPERIENCE TODAY.
CHOOSE ONE DISCUSSION STARTER
TO SHARE YOUR THOUGHTS.**



Discussion starters

I think...

It reminds me of...

I predict...

I noticed...


I like...



QUESTIONS

Contact Information

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Please
complete
the
Survey

